

Ground Rules for MA 265, Spring 2019

Course Webpage: <http://www.math.purdue.edu/courses/MA26500>.

Homework: The primary way to submit homework is through BLACKBOARD. The login page to BLACKBOARD is: <https://mycourses.purdue.edu>. There are also handwritten homework assignments which need to be turned in to your instructor and will be hand graded.

Midterm Examinations: There will be two midterm exams. Details of exams will be determined by your instructor.

Final Examination: There will be a two-hour, comprehensive final exam during finals week. The time and place will be announced later. The final exam will be **multiple choice**.

Grades: Course grades will be determined from your total score which will be computed as follows:

| | |
|------------------------|-------------|
| Homework | 25% |
| Two midterms, 20% each | 40% |
| Final Exam | 35% |
| Total Score | 100% |

Assignment of the grade:

- (1) The number of particular letter grades (A, B, . . .) in each section is based on the Final Exam Score across all sections of the course by using a coursewide Final Exam curve.
- (2) The letter grades within each section are then determined based on the **Total Score**.

Calculators: Calculators will not be allowed on exams. All computations in the course can be done by hand.

Attendance: Class attendance is expected. Reading the sections in the textbook (by the student) ahead of time is recommended.

Accommodations for Students with Disabilities: Purdue University strives to make learning experiences accessible to all participants. If you anticipate or experience physical or academic barriers based on disability, you are encouraged to contact the Disability Resource Center at: drc@purdue.edu or by phone: 765-494-1247.

If you have been certified by the Disability Resource Center (DRC) as eligible for academic adjustments on exams or quizzes, see <http://www.math.purdue.edu/ada> for exam and quiz procedures for your mathematics course, or go to MATH 202 for paper copies. In the event that you are waiting to be certified by the DRC we encourage you to review our procedures prior to being certified. For all in-class accommodations, please see your instructor outside class hours, before or after class, or during office hours, to share your accommodation Memorandum for the current semester and discuss your accommodations as soon as possible.

Large print copies of the *Information Sheet* are available from MATH 202 upon request.

Academic Dishonesty: The Mathematics Department, following Purdue Policy, prohibits academic dishonesty. Violations will be punished to the maximum possible extent set forth in the Purdue Policy on academic dishonesty; see http://www.purdue.edu/studentregulations/student_conduct/regulations.html

Important Dates: Last day for a student to drop a course

-without it being recorded: Monday, January 21st, 2019.

-without a grade: Monday, February 4th, 2019.

-with a passing or failing grade: Friday, March 8th, 2019.

PROBLEM LIST FOR MATH 265, SPRING 2019

BOOK = LINEAR ALGEBRA AND ITS APPLICATIONS, 5TH EDITION
BY DAVID C. LAY, STEVEN R. LAY AND JUDI J. MCDONALD

HANDWRITTEN PROBLEMS: TURN IN AT CLASS TIME

ONLINE HOMEWORK PROBLEMS: THROUGH BLACKBOARD AT
[HTTPS://WWW.MYCOURSES.PURDUE.EDU](https://www.mycourses.purdue.edu)

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- Lesson 2 : Section 1.2: Page 22 # 12, Page 23 # 25, 31
- Lesson 3 : Section 1.3: Page 33 # 23, 25
- Lesson 4 : Section 1.4: Page 40 # 6, Page 41 #26
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- Lesson 6 : Section 1.7: Page 62 # 26, 28, 32
- Lesson 7 : Section 1.8: Page 70 # 20, 22 (exclude e)
- Lesson 8 : Section 1.9: Page 80 # 28, 30
- Lesson 9 : Section 2.1: Page 103 # 18, 28
- Lesson 10: Section 2.2, 2.3: Page 112 # 19, Page 117 # 13
- Lesson 11: Section 2.8: Page 153 # 2, 18
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- Lesson 18: Section 4.3: Page 216 # 28, Page 217 # 34
- Lesson 19: Section 4.5: Page 231 # 20, 26
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- Lesson 21: Section 5.1: Page 274 # 20, Page 275 # 36
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- Lesson 26: Appendix B: HW#26 (posted on course website)
- Lesson 27: Section 5.5: Page 303 # 24

- Lesson 28: Section 5.7: Page 320 # 10
- Lesson 29: Section 5.7: Page 320 # 14
- Lesson 30: Section 6.1: Page 339 # 24, 26
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